

# Cubes And Cube Roots

## Ex. 6.1



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1.  $(-6)^3 = (-6) \times (-6) \times (-6) = -216$  (C)

2.  $(40)^3 = 40 \times 40 \times 40 = 64000$  (D)

3.  $\left(\frac{-5}{11}\right)^3 = \left(\frac{-5}{11}\right) \times \left(\frac{-5}{11}\right) \times \left(\frac{-5}{11}\right) = \frac{-125}{1331}$  (B)

4.  $(0.3)^3 = 0.3 \times 0.3 \times 0.3 = 0.027$  (D)

5.  $\left(3 - \frac{1}{3}\right)^3 = \left(\frac{9-1}{3}\right)^3 = \left(\frac{8}{3}\right)^3 = \frac{8}{3} \times \frac{8}{3} \times \frac{8}{3} = \frac{512}{27}$  (B)

6. (D) is false as cube of a number ending with zero has three zeroes at its extreme right.

7a.  $(25)^3 = 25 \times 25 \times 25 = 15625$

b.  $(18)^3 = 18 \times 18 \times 18 = 5832$

c.  $(63)^3 = 63 \times 63 \times 63 = 250047$

d.  $(133)^3 = 133 \times 133 \times 133 = 2352637$

8a.  $\left(-\frac{2}{3}\right)^3 = \left(-\frac{2}{3}\right) \times \left(-\frac{2}{3}\right) \times \left(-\frac{2}{3}\right) = \frac{-8}{27}$

b.  $\left(\frac{6}{19}\right)^3 = \frac{6}{19} \times \frac{6}{19} \times \frac{6}{19} = \frac{216}{6859}$

$$c. \left(-\frac{7}{15}\right)^3 = \left(-\frac{7}{15}\right) \times \left(-\frac{7}{15}\right) \times \left(-\frac{7}{15}\right) = \frac{-343}{3375}$$

$$d. \left(\frac{12}{24}\right)^3 = \left(\frac{1}{2}\right)^3 = \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} = \frac{1}{8}$$

$$9a. (0.1)^3 = 0.1 \times 0.1 \times 0.1 = 0.001$$

$$b. (0.02)^3 = 0.02 \times 0.02 \times 0.02 = 0.000008$$

$$c. (0.5)^3 = 0.5 \times 0.5 \times 0.5 = 0.125$$

$$d. (1.3)^3 = 1.3 \times 1.3 \times 1.3 = 2.197$$

$$10a. \begin{array}{r} 2 \overline{) 100} \\ \underline{2 \quad 50} \\ 5 \overline{) 25} \\ \underline{5 \quad 25} \\ 5 \end{array}$$

$$100 = 2 \times 2 \times 5 \times 5$$

Since 2 and 5 do not occur in a triplet.

$\therefore 100$  is not a perfect cube.

$$b. \begin{array}{r} 2 \overline{) 27000} \\ \underline{2 \quad 13500} \\ 2 \overline{) 6750} \\ \underline{3 \quad 3375} \\ 3 \overline{) 1125} \\ \underline{3 \quad 75} \\ 375 \end{array}$$

$$\begin{array}{r}
 3 \overline{) 375} \\
 \underline{5} \phantom{0} \\
 5 \overline{) 125} \\
 \underline{5} \phantom{0} \\
 5 \overline{) 25} \\
 \underline{5} \\
 5
 \end{array}$$

$$27000 = \underline{2 \times 2 \times 2} \times \underline{3 \times 3 \times 3} \times \underline{5 \times 5 \times 5}$$

Since 2, 3 and 5 occur in a triplet  
 $\therefore$  27000 is a perfect cube.

c.

$$\begin{array}{r}
 2 \overline{) 4096} \\
 \underline{2} \phantom{000} \\
 2 \overline{) 2048} \\
 \underline{2} \phantom{000} \\
 2 \overline{) 1024} \\
 \underline{2} \phantom{000} \\
 2 \overline{) 512} \\
 \underline{2} \phantom{000} \\
 2 \overline{) 256} \\
 \underline{2} \phantom{000} \\
 2 \overline{) 128} \\
 \underline{2} \phantom{000} \\
 2 \overline{) 64} \\
 \underline{2} \phantom{000} \\
 2 \overline{) 32} \\
 \underline{2} \phantom{000} \\
 2 \overline{) 16} \\
 \underline{2} \phantom{000} \\
 2 \overline{) 8} \\
 \underline{2} \phantom{000} \\
 2 \overline{) 4} \\
 \underline{2} \\
 2
 \end{array}$$

$$4096 = \underline{2 \times 2 \times 2} \times \underline{2 \times 2 \times 2} \times \underline{2 \times 2 \times 2} \times \underline{2 \times 2 \times 2}$$

Since 2 occurs in a triplet  
 $\therefore$  4096 is a perfect cube.

d.

$$\begin{array}{r}
 2 \overline{) 2430} \\
 \underline{3} \phantom{00} \\
 3 \overline{) 1215} \\
 \underline{3} \phantom{00} \\
 3 \overline{) 405} \\
 \underline{3} \phantom{00} \\
 3 \overline{) 135} \\
 \underline{3} \phantom{00} \\
 45
 \end{array}$$

$$\begin{array}{r} 3 \overline{) 45} \\ 3 \overline{) 15} \\ 5 \end{array}$$

$$2430 = 2 \times \underline{3 \times 3 \times 3 \times 3 \times 3} \times 5$$

Since 2, 3 and 5 do not occur in a triplet.

$\therefore$  2430 is not a perfect cube.

e.

$$\begin{array}{r} 19 \overline{) 6859} \\ 19 \overline{) 361} \\ 19 \end{array}$$

$$6859 = \underline{19 \times 19 \times 19}$$

Since 19 occurs in a triplet

$\therefore$  6859 is a perfect cube.

f.

$$\begin{array}{r} 5 \overline{) 15625} \\ 5 \overline{) 3125} \\ 5 \overline{) 625} \\ 5 \overline{) 125} \\ 5 \overline{) 25} \\ 5 \end{array}$$

$$15625 = \underline{5 \times 5 \times 5 \times 5 \times 5 \times 5}$$

Since 5 occurs in a triplet

$\therefore$  15625 is a perfect cube.

11.a.

$$\begin{array}{r} 2 \overline{) 1372} \\ 2 \overline{) 686} \\ 7 \overline{) 343} \\ 7 \overline{) 49} \\ 7 \end{array}$$

$$1372 = 2 \times 2 \times 7 \times 7 \times 7$$

Since 2 does not occur in a triplet  
 $\therefore$  We multiply 1372 by 2 to make it a perfect cube.

$\therefore$  Required smallest number = 2

b.

2	10584
2	5292
2	2646
3	1323
3	441
3	147
7	49
	7

$$10584 = 2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 7 \times 7$$

Since 7 does not occur in a triplet  
 $\therefore$  We multiply 10584 by 7 to make it a perfect cube.

$\therefore$  Required smallest number = 7

c.

3	1125
3	375
5	125
5	25
	5

$$1125 = 3 \times 3 \times 5 \times 5 \times 5$$

Since 3 does not occur in a triplet  
 $\therefore$  We multiply 1125 by 3 to make it a perfect cube

$\therefore$  Required smallest number = 3

12.a.

$$\begin{array}{r} 5 \overline{) 3125} \\ 5 \quad 625 \\ 5 \quad 125 \\ 5 \quad 25 \\ \hline 5 \end{array}$$

$$3125 = \underline{5 \times 5 \times 5 \times 5 \times 5}$$

Since 5 does not occur in a triplet

$\therefore$  We divide 3125 by  $5 \times 5 = 25$  to make it a perfect cube.

$\therefore$  Required smallest number = 25

b.

$$\begin{array}{r} 2 \overline{) 5324} \\ 2 \quad 2662 \\ 11 \quad 1331 \\ 11 \quad 121 \\ \hline 11 \end{array}$$

$$5324 = 2 \times 2 \times \underline{11 \times 11 \times 11}$$

Since 2 does not occur in a triplet

$\therefore$  We divide 5324 by  $2 \times 2 = 4$  to make it a perfect cube.

$\therefore$  Required smallest number = 4

c.

$$\begin{array}{r} 2 \overline{) 7290} \\ 3 \overline{) 3645} \\ 3 \overline{) 1215} \\ 3 \overline{) 405} \\ \hline 135 \end{array}$$

$$\begin{array}{r|l} 3 & 135 \\ \hline 3 & 45 \\ \hline 3 & 15 \\ \hline & 5 \end{array}$$

$$7290 = 2 \times \underline{3 \times 3 \times 3} \times \underline{3 \times 3 \times 3} \times 5$$

Since 2 and 5 do not occur in a triplet.

$\therefore$  We divide 7290 by  $2 \times 5 = 10$  to make it a perfect cube.

$\therefore$  Required smallest number = 10