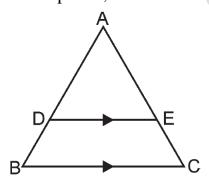
Basic Concepts

- 1. Two figures having the same shape but not necessarily the same size are called similar figures.
- 2. All the congruent figures are similar but the converse is not true.
- 3. Two polygons of the same number of sides are similar, if
- (i) Their corresponding angles are equal
- (ii) Their corresponding sides are in the same ratio (i.e., proportion)
- 4. Two triangles are similar, if
- (i) Their corresponding angles are equal.
- (ii) Their corresponding sides are in the same ratio (or proportion)

5. Basic Proportionality Theorem (B.P.T.) (Thales Theorem)

In a triangle, a line drawn parallel to one side, to intersect the other sides in distinct points, divides the two sides in the same ratio.



In $\triangle ABC$, if $DE \parallel BC$ then

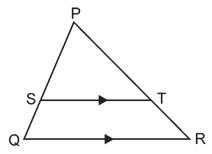
(i)
$$\frac{AD}{DB} = \frac{AE}{EC}$$

(ii)
$$\frac{AB}{AD} = \frac{AC}{AE}$$

(iii)
$$\frac{AB}{DB} = \frac{AC}{EC}$$

6. Converse of Basic Proportionality Theorem

If a line divides any two sides of a triangle in the same ratio, the line is parallel to the third side.

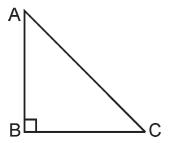


In
$$\triangle PQR$$
, if $\frac{PS}{SQ} = \frac{PT}{TR}$, then $ST \parallel QR$.

- 7. If in two triangles, corresponding angles are equal, then their corresponding sides are in the same ratio and hence the two triangles are similar (*AAA similarity criterion*).
- 8. If in two triangles, two angles of one triangle are respectively equal to the angles of the other triangle, then the two triangles are similar (*AA similarity criterion*).
- 9. If in two triangles, corresponding sides are in the same ratio, then their corresponding angles are equal and hence the triangles are similar (SSS similarity criterion).
- 10.If one angle of a triangle is equal to one angle of another triangle and the sides including these angles are in the same ratio (proportional), then the triangles are similar (*SAS similarity criterion*).
- 11.If a perpendicular is drawn from the vertex of the right angle of a right triangle to the hypotenuse, then the triangles on both sides of the perpendicular are similar to the whole triangle and also to each other.
- 12. The ratio of the areas of two similar triangles are equal to the ratio of the squares of any two corresponding sides.
- 13. The areas of two similar triangles are in the ratio of the squares of the corresponding altitudes.
- 14. The areas of two similar triangles are int eh ratio of the squares of the corresponding medians.
- 15. If the areas of two similar triangles are equal, then the triangles are congruent, i.e., equal and similar triangles are congruent.

$16. \\ \textbf{Pythagoras theorem}$

In a right triangle, the square of the hypotenuse is equal to the sum of the squares of the other two sides. In figure, $\angle B = 90^{\circ}$, so $AC^2 = AB^2 + BC^2$.



17. Converse of Pythagoras theorem

In a triangle, if the square of one side is equal to the sum of the squares of the other two sides, then the angle opposite to the first side is a right angle.