

1. Find the value of $\left(x - \frac{1}{x}\right)^3$ if $x = 1 + \sqrt{2}$
2. Evaluate: $125^{-\frac{1}{3}} \left(125^{\frac{1}{3}} - 125^{\frac{2}{3}}\right)$
3. If $x = \frac{1}{2-\sqrt{3}}$, find the value of $2x^3 - 2x^2 - 7x + 5$
4. Simplify: $\frac{2\sqrt{6}}{\sqrt{2}+\sqrt{3}} + \frac{6\sqrt{2}}{\sqrt{6}+\sqrt{3}} - \frac{8\sqrt{3}}{\sqrt{6}+\sqrt{2}}$
5. $a = \frac{\sqrt{3}+1}{\sqrt{3}-1}$ and $b = \frac{1}{a}$, find the value of $a^2 + ab - b^2$
6. Express $0.15\bar{9}$ in the form of $\frac{p}{q}$, where p and q are integers and $q \neq 0$.
7. If $x = 3 + 2\sqrt{2}$, then find the value of $\left(x - \frac{1}{x}\right)^3$
8. If $x = 9 + 4\sqrt{5}$, find the value of $\sqrt{x} - \frac{1}{\sqrt{x}}$
9. Simplify: $\frac{1}{1+\sqrt{2}} + \frac{1}{\sqrt{2}+\sqrt{3}} + \frac{2}{\sqrt{3}+\sqrt{5}}$
10. If $x = \frac{\sqrt{3}+\sqrt{2}}{\sqrt{3}-\sqrt{2}}$ and $y = \frac{\sqrt{3}-\sqrt{2}}{\sqrt{3}+\sqrt{2}}$, find the value of $x^2 + y^2 + xy$.