

1. Prove that:  $\frac{1}{1+\sqrt{2}} + \frac{1}{\sqrt{2}+\sqrt{3}} + \frac{1}{\sqrt{3}+\sqrt{4}}$  is a rational number.
2. Simplify:  $3\sqrt[3]{40} - 4\sqrt[3]{320} - \sqrt[3]{5}$
3. Solve:  $0.\bar{6} + 0.4\bar{7}$
4. Represent  $\sqrt{2}$  on the number line.
5. Evaluate:  $\frac{7\sqrt{3}}{\sqrt{10}+\sqrt{3}} - \frac{3\sqrt{2}}{\sqrt{15}+3\sqrt{2}} - \frac{2\sqrt{5}}{\sqrt{6}+\sqrt{5}}$
6. Evaluate:  $\frac{\left(\frac{9}{4}\right)^{-\frac{3}{2}} \times \left(\frac{125}{27}\right)^{-\frac{2}{3}} \times \left(\frac{3}{5}\right)^{-2}}{(\sqrt{2})^4}$
7. If  $x^a = y$ ,  $y^b = z$  and  $z^c = x$ , then prove that  $abc = 1$ .
8. Write in simplest form:  $8\sqrt{45} + 2\sqrt{50} - 3\sqrt{147}$
9. Simplify:  $\left[5^2 \left(8^{\frac{1}{3}} + 27^{\frac{1}{3}}\right)^3\right]^{\frac{1}{5}}$
10. Express  $0.\overline{235}$  in the form  $\frac{p}{q}$  where  $p$  and  $q$  are integers,  $q \neq 0$ .